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**Clarence W. Wilkerson\*** (cwilkers@purdue.edu), Clarence W. Wilkerson, Dept. Math,  
Purdue University, est Lafayette, IN 47907. *Poincare' duality algebras as rings of  
coinvariants*. Preliminary report.

If  $V$  is a finite dimensional vector space over a field  $k$ , and  $W$  is a finite subgroup of  $Aut(V)$ , then the symmetric algebra  $S(V^\#)$  can be thought of as the algebra of polynomial functions on  $V$ , and it inherits an action of the group  $W$ . The algebra of invariants  $S(V^\#)^W$  is of particular interest. If it is itself a polynomial algebra, then the quotient algebra  $S(V^\#)/I$ , where  $I$  is the ideal generated by the positive degree elements of  $S(V^\#)^W$  form the coinvariants and is Poincare' duality algebra under the induced multiplication.

However, if the characteristic of  $k$  is positive, the coinvariants can be a Poincare duality algebra without  $S(V^\#)^W$  being polynomial. The author and W. G. Dwyer give a generic example of this behavior. Moreover, we give a new proof, independent of the previous work of Steinberg, Kane, and T.C. Lin of the following theorem.

With notation as above, if  $\text{char}(k) = 0$  or  $p$  with  $p$  relatively prime to the order of  $W$ , then  $S(V^\#)/I$  is a Poincare' duality algebra if and only if  $S(V^\#)^W$  is a polynomial algebra.

This is joint work with W. G. Dwyer, Notre Dame (Received February 14, 2006)