Sorting integer arrays: security, speed, and verification

1

D. J. Bernstein

University of Illinois at Chicago, Ruhr-University Bochum

Bob's laptop screen:

From: Alice

Thank you for your submission. We received many interesting papers, and unfortunately your

Bob assumes this message is something Alice actually sent.

But today's "security" systems fail to guarantee this property. Attacker could have modified or forged the message.

Trusted computing base (TCB)

TCB: portion of computer system that is responsible for enforcing the users' security policy.

Trusted computing base (TCB)

TCB: portion of computer system that is responsible for enforcing the users' security policy.

Bob's security policy for this talk: If message is displayed on Bob's screen as "From: Alice" then message is from Alice.

Trusted computing base (TCB)

TCB: portion of computer system that is responsible for enforcing the users' security policy.

Bob's security policy for this talk: If message is displayed on Bob's screen as "From: Alice" then message is from Alice.

If TCB works correctly, then message is guaranteed to be from Alice, no matter what the rest of the system does.

 Attacker uses buffer overflow in a device driver to control Linux kernel on Alice's laptop.

- Attacker uses buffer overflow in a device driver to control Linux kernel on Alice's laptop.
- Attacker uses buffer overflow
 in a web browser to control
 disk files on Bob's laptop.

- Attacker uses buffer overflow in a device driver to control Linux kernel on Alice's laptop.
- Attacker uses buffer overflow in a web browser to control disk files on Bob's laptop.

Device driver is in the TCB. Web browser is in the TCB. CPU is in the TCB. Etc.

- Attacker uses buffer overflow in a device driver to control Linux kernel on Alice's laptop.
- Attacker uses buffer overflow in a web browser to control disk files on Bob's laptop.

Device driver is in the TCB. Web browser is in the TCB. CPU is in the TCB. Etc.

Massive TCB has many bugs, including many security holes. Any hope of fixing this?

Rearchitect computer systems to have a much smaller TCB.

Rearchitect computer systems to have a much smaller TCB.

Carefully audit the TCB.

Rearchitect computer systems to have a much smaller TCB.

Carefully audit the TCB.

e.g. Bob runs many VMs:



VM	С
Charlie	data

TCB stops each VM from touching data in other VMs.

Rearchitect computer systems to have a much smaller TCB.

Carefully audit the TCB.

e.g. Bob runs many VMs:



TCB stops each VM from touching data in other VMs.

Browser in VM C isn't in TCB. Can't touch data in VM A, if TCB works correctly.

Rearchitect computer systems to have a much smaller TCB.

Carefully audit the TCB.

e.g. Bob runs many VMs:



TCB stops each VM from touching data in other VMs.

Browser in VM C isn't in TCB. Can't touch data in VM A,

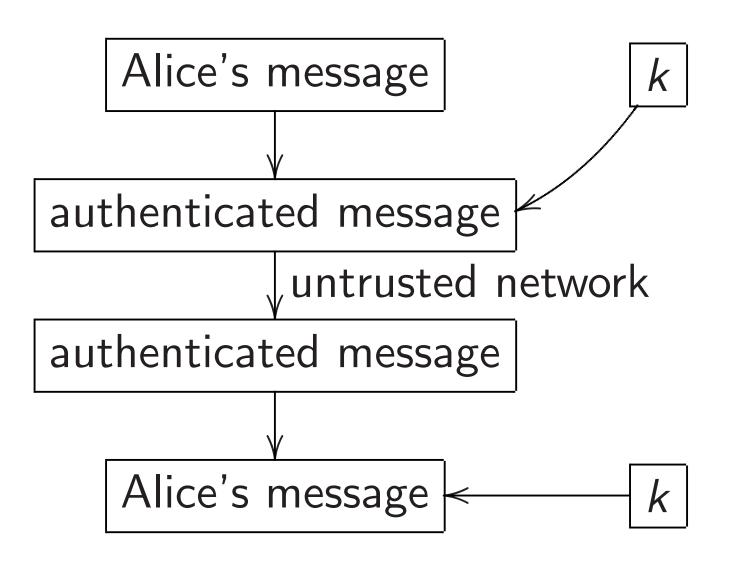
if TCB works correctly.

Alice also runs many VMs.

<u>Cryptography</u>

How does Bob's laptop know that incoming network data is from Alice's laptop?

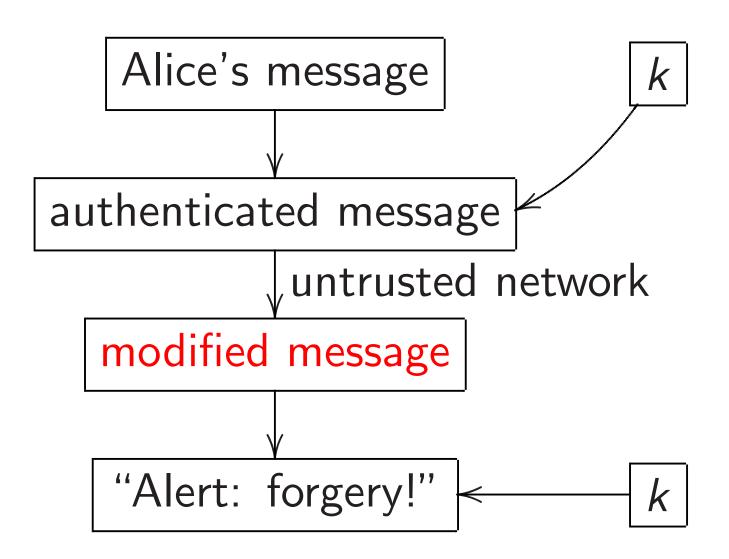
Cryptographic solution: Message-authentication codes.



<u>Cryptography</u>

How does Bob's laptop know that incoming network data is from Alice's laptop?

Cryptographic solution: Message-authentication codes.



Important for Alice and Bob to share the same secret k.

7

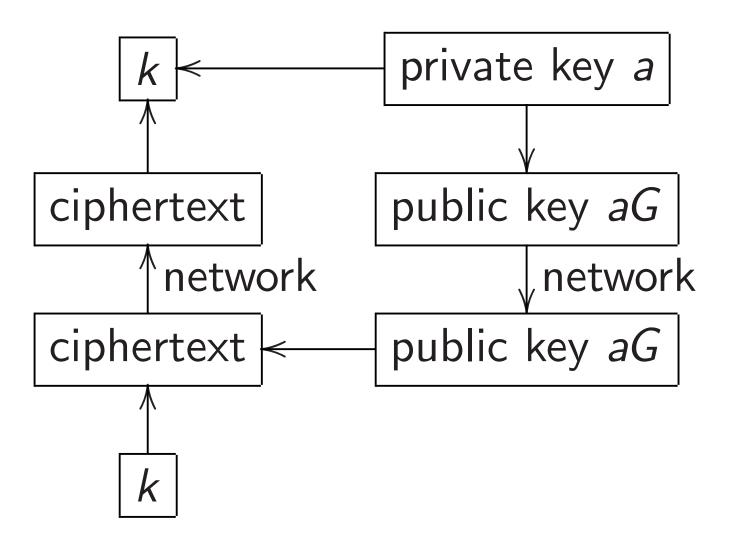
What if attacker was spying on their communication of *k*?

Important for Alice and Bob to share the same secret k.

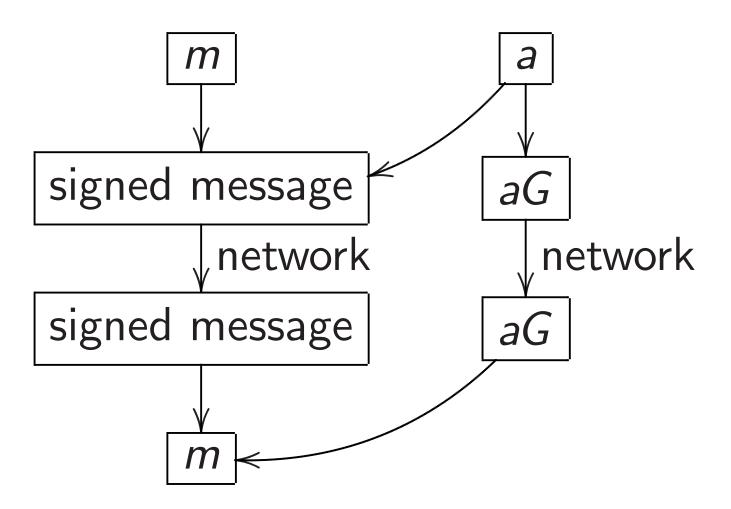
What if attacker was spying on their communication of *k*?

Solution 1:

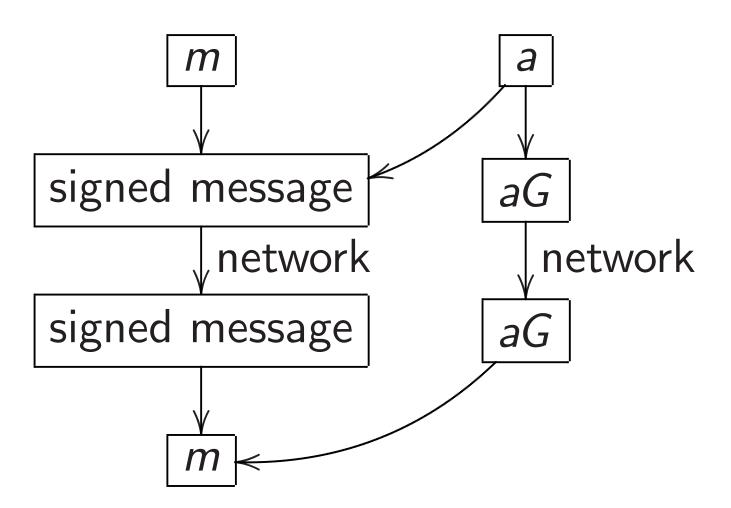
Public-key encryption.



Solution 2: Public-key signatures.



Solution 2: Public-key signatures.



No more shared secret k but Alice still has secret a. **Cryptography requires TCB to protect secrecy of keys,** even if user has no other secrets.

Constant-time software

Large portion of CPU hardware: optimizations depending on addresses of memory locations.

Consider data caching, instruction caching, parallel cache banks, store-to-load forwarding, branch prediction, etc.

Constant-time software

Large portion of CPU hardware: optimizations depending on addresses of memory locations.

Consider data caching, instruction caching, parallel cache banks, store-to-load forwarding, branch prediction, etc.

Many attacks show that this portion of the CPU has trouble keeping secrets. e.g. RIDL: 2019 Schaik–Milburn–Österlund–Frigo– Maisuradze–Razavi–Bos–Giuffrida. Typical literature on this topic:

Understand this portion of CPU. But details are often proprietary, not exposed to security review.

Try to push attacks further. This becomes very complicated.

Tweak the attacked software to try to stop the known attacks.

Typical literature on this topic:

Understand this portion of CPU. But details are often proprietary, not exposed to security review.

Try to push attacks further. This becomes very complicated.

Tweak the attacked software to try to stop the known attacks.

For researchers: This is great!

Typical literature on this topic:

Understand this portion of CPU. But details are often proprietary, not exposed to security review.

Try to push attacks further. This becomes very complicated.

Tweak the attacked software to try to stop the known attacks.

For researchers: This is great!

For auditors: This is a nightmare. Many years of security failures. No confidence in future security. The "constant-time" solution: Don't give any secrets to this portion of the CPU. (1987 Goldreich, 1990 Ostrovsky: Oblivious RAM; 2004 Bernstein: domain-specific for better speed) 11

The "constant-time" solution: Don't give any secrets to this portion of the CPU. (1987 Goldreich, 1990 Ostrovsky: **Oblivious RAM: 2004 Bernstein:** domain-specific for better speed) TCB analysis: Need this portion of the CPU to be correct, but don't need it to keep secrets. Makes auditing much easier.

11

The "constant-time" solution: Don't give any secrets to this portion of the CPU. (1987 Goldreich, 1990 Ostrovsky: **Oblivious RAM: 2004 Bernstein:** domain-specific for better speed) TCB analysis: Need this portion of the CPU to be correct, but don't need it to keep secrets. Makes auditing much easier.

11

Good match for attitude and experience of CPU designers: e.g., Intel issues errata for correctness bugs, not for information leaks.

Case study: Constant-time sorting

Serious risk within 10 years: Attacker has quantum computer breaking today's most popular public-key crypto (RSA and ECC; e.g., finding *a* given *aG*).

Case study: Constant-time sorting

Serious risk within 10 years: Attacker has quantum computer breaking today's most popular public-key crypto (RSA and ECC; e.g., finding *a* given *aG*).

2017: Hundreds of people submit 69 complete proposals to international competition for post-quantum crypto standards.

Case study: Constant-time sorting

Serious risk within 10 years: Attacker has quantum computer breaking today's most popular public-key crypto (RSA and ECC; e.g., finding *a* given *aG*).

2017: Hundreds of people submit 69 complete proposals to international competition for post-quantum crypto standards.

Subroutine in some submissions: sort array of secret integers. e.g. sort 768 32-bit integers.

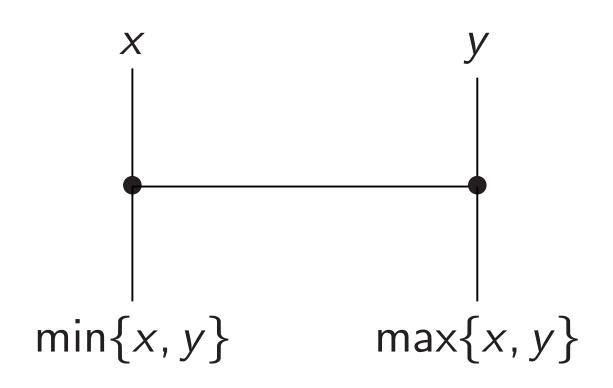
Typical sorting algorithms merge sort, quicksort, etc. choose load/store addresses based on secret data. Usually also branch based on secret data.

Typical sorting algorithms merge sort, quicksort, etc. choose load/store addresses based on secret data. Usually also branch based on secret data.

One submission to competition: "Radix sort is used as constant-time sorting algorithm." Some versions of radix sort avoid secret branches.

Typical sorting algorithms merge sort, quicksort, etc. choose load/store addresses based on secret data. Usually also branch based on secret data.

One submission to competition: "Radix sort is used as constant-time sorting algorithm." Some versions of radix sort avoid secret branches. But data addresses in radix sort still depend on secrets. Foundation of solution: a **comparator** sorting 2 integers.

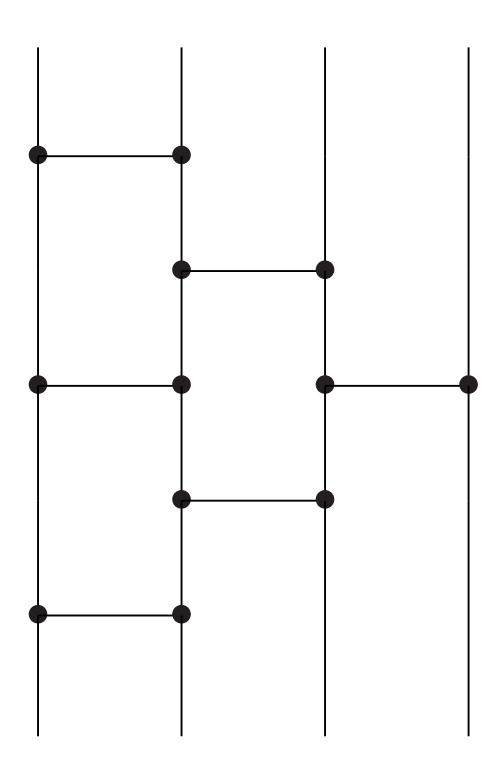


Easy constant-time exercise in C. Warning: C standard allows compiler to screw this up.

Even easier exercise in asm.

Combine comparators into a **sorting network** for more inputs.

Example of a sorting network:



Positions of comparators in a sorting network are independent of the input. Naturally constant-time. Positions of comparators in a sorting network are independent of the input. Naturally constant-time.

But $(n^2 - n)/2$ comparators produce complaints about performance as *n* increases. Positions of comparators in a sorting network are independent of the input. Naturally constant-time.

But $(n^2 - n)/2$ comparators produce complaints about performance as *n* increases.

Speed is a serious issue in the post-quantum competition. "Cost" is evaluation criterion; "we'd like to stress this once again on the forum that we'd really like to see more platformoptimized implementations"; etc. void int32_sort(int32 *x,int64 n) { int64 t,p,q,i; if (n < 2) return; t = 1;while (t < n - t) t += t;for (p = t;p > 0;p >>= 1) { for (i = 0; i < n - p; ++i)if (!(i & p)) minmax(x+i,x+i+p); for (q = t; q > p; q >>= 1)for (i = 0; i < n - q; ++i)if (!(i & p)) minmax(x+i+p,x+i+q); }

17

Previous slide: C translation of 1973 Knuth "merge exchange", which is a simplified version of 1968 Batcher "odd-even merge" sorting networks.

 $\approx n(\log_2 n)^2/4$ comparators. Much faster than bubble sort.

Warning: many other descriptions of Batcher's sorting networks require *n* to be a power of 2. Also, Wikipedia says "Sorting networks are not capable of handling arbitrarily large inputs."

This constant-time sorting code

vectorization (for Haswell)

Constant-time sorting code included in 2017 Bernstein–Chuengsatiansup– Lange-van Vredendaal "NTRU Prime" software release revamped for higher speed New: djbsort constant-time sorting code

The slowdown for constant time

How much speed did we lose by refusing to use variable-time quicksort, radix sort, etc.?

Cycles on Intel Haswell CPU core to sort n = 768 32-bit integers:

26948 stdsort (variable-time) 22812 herf (variable-time) 17748 krasnov (variable-time) 16980 ipp 2019.5 (variable-time) 12672 sid1607 (variable-time)

The slowdown for constant time

How much speed did we lose by refusing to use variable-time quicksort, radix sort, etc.?

Cycles on Intel Haswell CPU core to sort n = 768 32-bit integers:

26948 stdsort (variable-time)
22812 herf (variable-time)
17748 krasnov (variable-time)
16980 ipp 2019.5 (variable-time)
12672 sid1607 (variable-time)
5964 djbsort (constant-time)

The slowdown for constant time

How much speed did we lose by refusing to use variable-time quicksort, radix sort, etc.?

Cycles on Intel Haswell CPU core to sort n = 768 32-bit integers:

26948 stdsort (variable-time)
22812 herf (variable-time)
17748 krasnov (variable-time)
16980 ipp 2019.5 (variable-time)
12672 sid1607 (variable-time)
5964 djbsort (constant-time)

No slowdown. New speed records!

How can an $n(\log n)^2$ algorithm beat standard $n \log n$ algorithms?

How can an *n*(log *n*)² algorithm beat standard *n* log *n* algorithms?

Answer: well-known trends in CPU design, reflecting fundamental hardware costs of various operations. How can an *n*(log *n*)² algorithm beat standard *n* log *n* algorithms?

Answer: well-known trends in CPU design, reflecting fundamental hardware costs of various operations.

Every cycle, Haswell core can do 8 "min" ops on 32-bit integers + 8 "max" ops on 32-bit integers. How can an *n*(log *n*)² algorithm beat standard *n* log *n* algorithms?

Answer: well-known trends in CPU design, reflecting fundamental hardware costs of various operations.

Every cycle, Haswell core can do 8 "min" ops on 32-bit integers + 8 "max" ops on 32-bit integers.

Loading a 32-bit integer from a random address: much slower.

Conditional branch: much slower.

<u>Verification</u>

Sorting software is in the TCB. Does it work correctly?

Test the sorting software on many random inputs, increasing inputs, decreasing inputs. Seems to work.

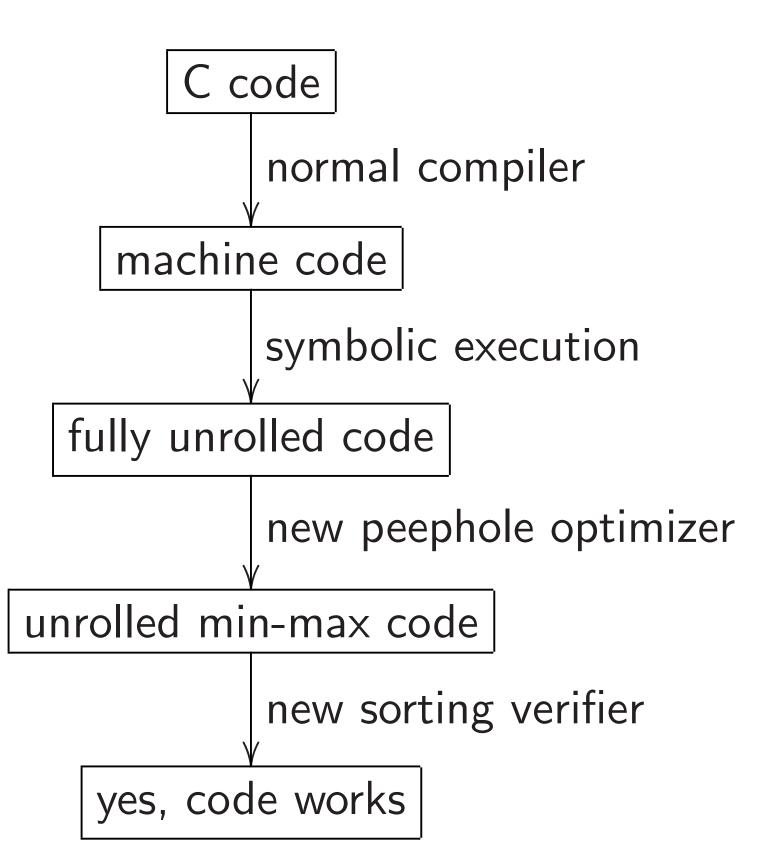
<u>Verification</u>

Sorting software is in the TCB. Does it work correctly?

Test the sorting software on many random inputs, increasing inputs, decreasing inputs. Seems to work.

But are there *occasional* inputs where this sorting software fails to sort correctly?

History: Many security problems involve occasional inputs where TCB works incorrectly. For each used n (e.g., 768):



Symbolic execution:

use existing angr.io toolkit, with several tiny new patches for eliminating byte splitting, adding a few missing vector instructions. Symbolic execution:

use existing angr.io toolkit, with several tiny new patches for eliminating byte splitting, adding a few missing vector instructions.

Peephole optimizer: recognize instruction patterns equivalent to min, max. Symbolic execution:

use existing angr.io toolkit, with several tiny new patches for eliminating byte splitting, adding a few missing vector instructions.

Peephole optimizer: recognize instruction patterns equivalent to min, max.

Sorting verifier: decompose DAG into merging networks. Verify each merging network using generalization of 2007 Even–Levi–Litman, correction of 1990 Chung–Ravikumar. Current djbsort release (verified fast int32 on AVX2, verified portable int32, fast uint32, fast float32):

sorting.cr.yp.to

Includes the sorting code; automatic build-time tests; simple benchmarking program; verification tools.

Web site shows how to use the verification tools.

Next release planned: verified ARM NEON code.