Better proofs for rekeying

## D. J. Bernstein

Security of AES-256 key k is far below  $2^{256}$  in most protocols:  $(AES_k(0), \ldots, AES_k(n-1))$  is distinguishable from uniform with probability  $n(n-1)/2^{129}$ , plus tiny key-guessing probability. Yes, distinguishers matter.

Attacker actually has T targets: independent keys  $k_1, \ldots, k_T$ . Success chance  $\approx T n(n-1)/2^{129}$ .

"Rekeying" seems less dangerous.

Expand k into  $F(k) = (AES_k(0), ..., AES_k(999999)).$ 

Split F(k) into 500000 "subkeys".

Output F(k') for each subkey k': i.e.,  $F(AES_k(0), AES_k(1))$ ;  $F(AES_k(2), AES_k(3))$ ; ...  $F(AES_k(999998), AES_k(999999)$ ). Better proofs for rekeying

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Crypto 2006 Bellare proof: more reasonable-sounding assumptions.

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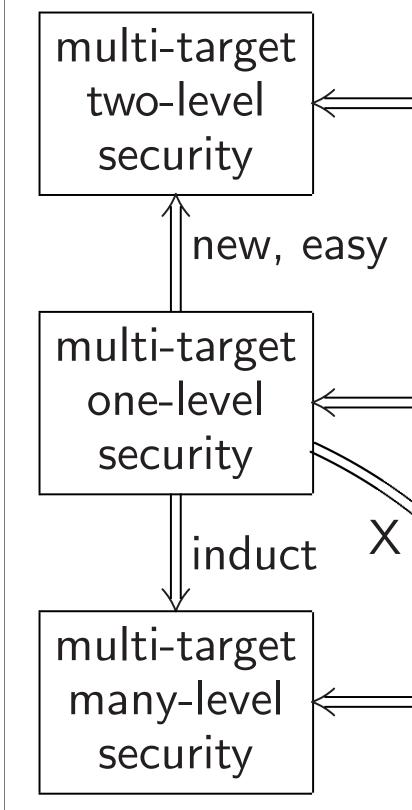
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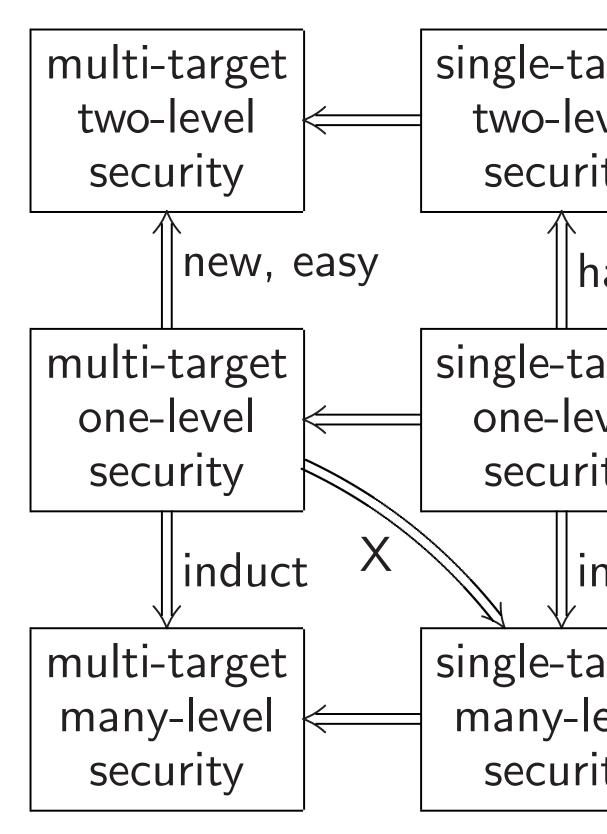
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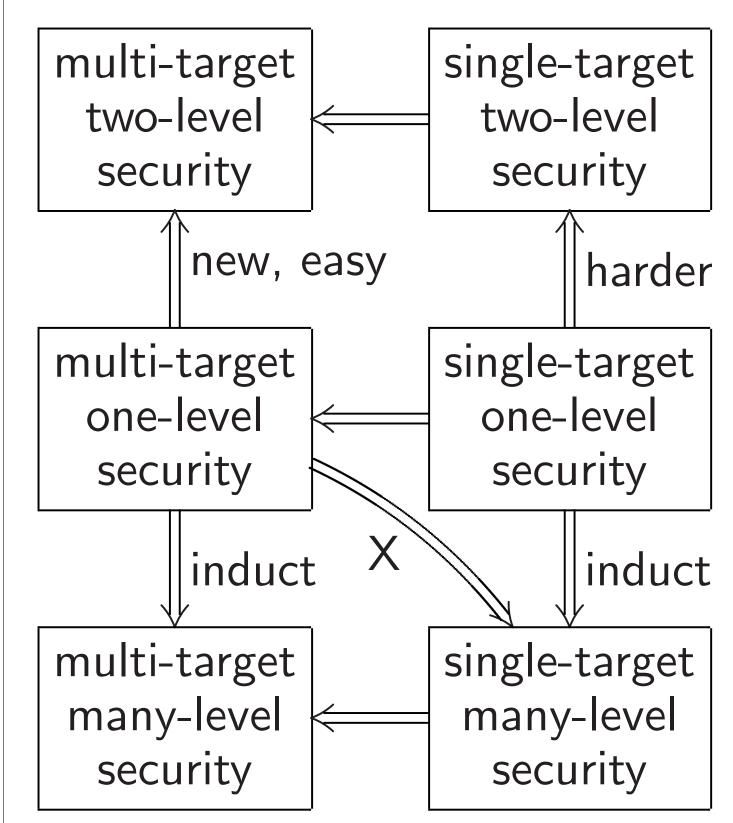
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