

1016-52-127

Ellen Veomett* (eveomett@umich.edu), University of Michigan, 2074 East Hall, 530 Church Street, Ann Arbor, MI 48109-1043. *Positive Semidefinite Approximations of Convex Bodies.*

Given an arbitrary convex body X , we construct a hierarchy of convex sets P_1, P_2, \dots each contained in X . Every P_k is obtained as an intersection of a cone of positive semidefinite quadratic forms with an affine space. If $X \subset \mathbb{R}^n$ is a 0-1 polytope, we can show that $P_n = X$, similar to construction results of Lasserre, Lovász and Schrijver, and Sherali and Adams. In the case where X is the traveling salesman polytope on n cities T_n , we can give metric bounds on the approximation. Namely, we show that if $k \leq \lfloor \frac{n}{2} \rfloor$ then the scaling of P_k by $\frac{n}{k} + O\left(\frac{1}{n}\right)$ contains T_n . Membership in P_k is computable in time polynomial in n , the degree of the polynomial linear in k . We also discuss facets of the traveling salesman polytope which lie on the boundary of P_k . (Received February 07, 2006)